

COMP 141

CS1: Programming Fundamentals



1

Announcements

Reminder

- Program 8 due Friday, April 27th by 11:55pm.

2

2-D List Lab from Last Time

Underlying Data Representation

- Remember back to the beginning of the semester
- We said that all data in a computer is stored in sequences of 0s and 1s
- **Byte**: just enough memory to store letter or small number
 - Divided into eight bits
 - **Bit**: electrical component that can hold positive or negative charge, like on/off switch
 - The on/off pattern of bits in a byte represents data stored in the byte

4

Binary Numbers

A Binary Number is made up of only **0s** and **1s**.

Example of a Binary Number

110100

There is no 2,3,4,5,6,7,8 or 9 in Binary!

5

How do we count using binary?

| Binary | |
|--------|--|
| 0 | We start at 0 |
| 1 | Then 1 |
| ??? | But then there is no symbol for 2...what do we do? |

6

How do we count in Decimal?

| Decimal | |
|---------|--|
| 0 | Start at 0 |
| ... | Count 1,2,3,4,5,6,7,8 |
| 9 | This is the last digit in Decimal |
| 10 | So we start back at 0 again, but add 1 on the left |

7

Applying to Binary

| | Binary | |
|------|--------|--|
| | 0 | We start at 0 |
| * | 1 | Then 1 |
| ** | 10 | Now we start back at 0, and add 1 to the left |
| *** | 11 | 1 more |
| **** | 100 | Start back at 0 again, and add one to the number on the left... ... but that number is already at 1 so it also goes back to 0 and 1 is added to the <i>next position</i> on the left |

8

Decimal vs. Binary

| Decimal: | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
|----------|---|---|----|----|-----|-----|-----|-----|------|------|------|------|------|------|------|------|
| Binary: | 0 | 1 | 10 | 11 | 100 | 101 | 110 | 111 | 1000 | 1001 | 1010 | 1011 | 1100 | 1101 | 1110 | 1111 |

| Decimal: | 20 | 25 | 30 | 40 | 50 | 100 | 200 | 500 |
|----------|-------|-------|-------|--------|--------|---------|----------|-----------|
| Binary: | 10100 | 11001 | 11110 | 101000 | 110010 | 1100100 | 11001000 | 111110100 |

"Binary is as easy as 1, 10, 11."

9

Binary Numbers

- Each position in a binary number represents 2^n

$$10111 = 1 * 2^4 + 0 * 2^3 + 1 * 2^2 + 1 * 2^1 + 1 * 2^0$$

$$101001 = 1 * 2^5 + 0 * 2^4 + 1 * 2^3 + 0 * 2^2 + 0 * 2^1 + 1 * 2^0$$

- This is the same as the decimal system:

$$193 = 1 * 10^2 + 9 * 10^1 + 3 * 10^0$$

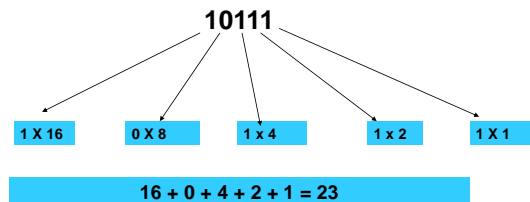
10

Converting Decimal to Binary

- $47 / 2 = 23 \text{ rem } 1$
- $23 / 2 = 11 \text{ rem } 1$
- $11 / 2 = 5 \text{ rem } 1$
- $5 / 2 = 2 \text{ rem } 1$
- $2 / 2 = 1 \text{ rem } 0$
- $1 / 2 = 0 \text{ rem } 1$
- Hence 47 in decimal format equals 101111 in binary format.

11

Converting Binary to Decimal



12

Adding Binary Numbers

$$\begin{array}{r} 10011 \\ + 1111 \\ \hline 100010 \end{array}$$

13

Practice

- Convert 39_{10} into binary
- Convert 1010110_2 into decimal

Practice

- Write 2 functions:
 - `toBinary(decimal)` – takes in a decimal number and returns its binary equivalent
 - `toDecimal(binary)` – takes in a binary number and returns its decimal equivalent
- **Hints:**
 - In `toDecimal`, you should convert binary to a string
 - In `toBinary`, you should create binary as a string, then typecast it to an integer before returning.
- Examples:


```
print(toBinary(1198)) #Prints 10010101110
print(toBinary(5))   #Prints 101

print(toDecimal(10001110)) #Prints 142
print(toDecimal(11))      #Prints 3
```

15