

Discrete Structures, Fall 2017, Homework 5

You must write the solutions to these problems legibly on your own paper, with the problems in sequential order, and with all sheets stapled together.

For each statement below, state whether it is true or false. Then prove the statement if it is true, or its negation if it is false.

Remember, an example may only be used to prove that an existential statement is true or a universal statement is false. Any example or counter-example must include specific values for the variables and enough algebra and justification to illustrate that the example proves what you are claiming it proves.

You do not need to translate each statement into symbols first, though it is often useful to do so.

1. The product of any two odd integers is odd.
2. For any integers a and b , if $a - b$ is even, then a and b are both even.
3. If n is an even integer, then $n^2 - 2$ is even.
4. The sum of an integer and a rational number is rational.
5. If n and m are rational numbers, then n/m is a rational number.

Hints: Remember, not all of these are necessarily true! Use the step-by-step example proofs from the handouts last week as a guide for these.