## Function definitions

Functions: the most important building block in the whole course

- Like C++ functions, have arguments and result
- But no classes, this, return, etc.

Example function binding:

```
(* Note: correct only if y>=0 *)
(define (pow x y)
    (if (= y 0)
        1
        (* x (pow x (- y 1)))))
```

Note: The body includes a (recursive) function call: pow ( $\mathbf{x}, \mathbf{y}-1$ )

## Example, extended

(define (pow x y)
(if (= y 0)
1
(* $\mathbf{x}$ (pow $\mathbf{x}(-\mathrm{y} 1)))$ )
(define (cube $x$ )
(pow x 3))
(define sixtyfour (cube 4))
(define fortytwo (+ (pow 2 4) (pow 42 ) (cube 2) 2)

## Recursion

- If you're not yet comfortable with recursion, you will be soon ©
- Will use for most functions taking or returning lists
- "Makes sense" because calls to same function solve "simpler" problems
- Recursion more powerful than loops
- Will not normally use loops in Racket (they exist, but are usually poor style.)
- Loops often (not always) obscure simple, elegant solutions


## Function bindings

- Syntax: (define (f x1 x2 . . . xn) b)
- (Will generalize in later lecture)
- $f$ is the name of the function.
- x1 through xn are the arguments (possibly none).
- $\mathbf{b}$ is an expression that is the body of the function.
- Evaluation: The name of a function is a value!
- Different than in many other programming languages.
- Adds $\mathbf{f}$ to environment so later expressions can call it.
- (Function-call semantics will also allow recursion.)


## Function Calls

A new kind of expression: 3 questions
Syntax: (e0 e1 . . . en)

- (Will generalize later)

Type-checking:

- e0 must evaluate to a function.


## Function-calls continued

(e0 e1 . . . en)

Evaluation:

1. (In current environment,) evaluate $\mathbf{e 0}$ to a function with arguments $\mathbf{x 1}, \ldots, \mathrm{xn}$, and body b .
2. (In current environment,) evaluate arguments to values v1, ..., vn
3. Result is evaluation of $b$ in an environment extended to map $\mathbf{x 1}$ to $\mathrm{v} 1, \ldots, \mathrm{xn}$ to vn

- ("An environment" is actually the environment where the function was defined, and includes $\mathbf{x 0}$ for recursion)


## Some gotchas

- Can't add extra parentheses like in Python/C++.
$-(+12)$ is fine... (+ (12)) is not fine, and neither is ((+ 12$)$ ).
- Parentheses have a very particular meaning in Scheme; they are not just used for changing precedence or grouping.
- Using prefix notation for everything pretty much eliminates having to use parens for precedence.
- No "return" statement.
- Functions only have a single expression as the body anyway.
- Evaluating that statement becomes the return value.


## Pairs and lists

So far: numbers, booleans (\#t and \#f), conditionals, variables, functions

- Now ways to build up data with multiple parts
- This is essential
- C++ examples: classes with fields, arrays

Rest of lecture:

- Pairs and lists
- These are our basic data structures that we use to create all other data structures.

Later: Other more general ways to create compound data

## Cons cells

- Fundamental data structure for Racket (and pretty much every other "parentheses-based" PL [Scheme, LISP])
- Two-piece structure:

- Left side is called the "car"
- Right side called the "cdr" (pronounced could-er)
- Each piece holds a pointer to something else (the something can be almost anything)


## Pairs

We need a way to build pairs and a way to access the pieces

Build:

- Syntax: (cons e1 e2)
- Evaluation: Evaluate e1 to v1 and e2 to v2; result is (v1 . v2)
- A pair of values is a value.
- Stored in a single cons cell.


## Pairs

We need a way to build pairs and a way to access the pieces

Build:

- Alternate syntax: ' (v1 . v2)
- Evaluation: No evaluation!
- This is how to make a "literal" pair, where v1 and v2 are not evaluated.
- Similar to using double quotes to make a string literal in Python/C++.
- E.g.: (cons (+ 12 ) (+ 34 )) makes the pair (3.7).
- E.g.: '(3.7) also makes the pair (3.7).
- E.g.: However, '((+ 12 ) . (+ 3 4)) makes the pair ((+ 12 ) . (+ 34 ))


## Pairs

We need a way to build pairs and a way to access the pieces
Access:

- Syntax: (car e) and (cdre)
- Evaluation: Evaluate e to a pair of values and return first or second piece
- Example: If $\mathbf{e}$ is a variable $\mathbf{x}$, then look up $\mathbf{x}$ in environment


## Examples

Functions can take and return pairs

```
(define (swap pair)
    (cons (cdr pair) (car pair)))
(define (sum-two-pairs p1 p2)
    (+ (car p1) (cdr p1) (car p2) (cdr p2)))
(define (div-mod n1 n2)
    (cons (quotient n1 n2) (remainder n1 n2)))
    ; returning more than one value is a pain in C++
(define (sort-pair pair)
    (if (> (car pair) (cdr pair))
        pair
        (swap pair)))
```


## Lists

- Lists are built in Racket using linked lists of cons cells.

Need ways to build lists and access the pieces...

## Building Lists

- The empty list is a value:


## '()

- In general, a list of values is a value; elements separated by spaces:
'(v1 v2 ...vn)
- If e1 evaluates to $\mathbf{v}$ and $\mathbf{e} 2$ evaluates to a list ( v 1 ... vn ), then (cons e1 e2) evaluates to (v v1 ... vn)


## Accessing Lists

- (null? e) evaluates to \#t if and only if e evaluates to ' ().
- If e evaluates to '(v1 v2 ... vn) then (car e) evaluates to v1
- (throw exception if e evaluates to ' ())
- If e evaluates to (v1 v2 ... vn) then (cdre) evaluates to (v2 ... vn)
- (throw exception if e evaluates to ' () )
- Notice result is a list


## Example list functions

```
(define (sum-list lst)
    (if (null? lst)
        0
        (+ (car lst) (sum-list (cdr lst)))))
    (define (countdown num)
    (if (= num 0)
        '()
        (cons num (countdown (- num 1)))))
```


## Recursion again

Functions over lists are usually recursive

- Only way to "get to all the elements"
- What should the answer be for the empty list?
- Usually, this is your base case.
- What should the answer be for a non-empty list?
- Typically in terms of the answer for the cdr of the list!

Similarly, functions that produce lists of potentially any size will be recursive

- You create a list out of smaller lists.


## Two other ways to build lists

- list function
- Makes a list out of all arguments.
- Arguments can be of any data type.
- (list e1 e2 ... en) evaluates e1 through en to values v1 through vn; returns the list ' (v1 v2 ... vn).
- append function
- Concatenates values inside lists given as arguments.
- Arguments must be lists.
- (append e1 e2 ... en) evaluates e1 through en to values v1 through vn;
- If $\mathbf{v} 1=(\mathrm{v} 11 \mathrm{v} 12 \ldots)$... and $\mathbf{v} 2=(\mathrm{v} 21 \mathrm{v} 22$... ) etc, then return value is (v11 v12 ... v21 v22 ... ).


## Lists of pairs

Processing lists of pairs requires no new features. Examples:

```
(define (sum-pair-list lst)
    (if (null? lst)
    O
        (+ (car (car lst)) (cdr (car lst)) (sum-pair-list (cdr lst)))))
(define (firsts lst)
    (if (null? lst)
        ()
        (cons (car (car lst)) (firsts (cdr lst)))))
(define (seconds lst)
    (if (null? lst)
        ()
        (cons (cdr (car lst)) (seconds (cdr lst)))))
(define (sum-pair-list2 lst)
    (+ (sum-list (firsts lst)) (sum-list (seconds lst))))
```

