

Programming Languages

Thunks, Laziness, Streams, Memoization

*Adapted from Dan Grossman's PL class,
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You've been lied to

- Everything that looks like a function call in Racket is not necessarily a function.
- Everything that looks like a function is either
 - A function call (as we thought)
 - Or a “special form”
- Special forms: define, let, lambda, if, cond, and, or, ...
- Why can't these be functions?
- Recall the evaluation model for a function call:
 - **(f e1 e2 e3...)**: evaluate **e1 e2 ...** to obtain values **v1 v2...**, then evaluate **f** to get a closure, then evaluate the code of the closure with its arguments bound to **v1 v2...**
 - Why would this not work for defining if?

Delayed evaluation

In Racket, function arguments are eager (call by value)

Special form arguments are lazy (call by need)

- Delay evaluation of the argument until we really need its value

Why wouldn't these functions work?

```
(define (my-if-bad x y z)
  (if x y z))
```

```
(define (fact-wrong n)
  (my-if-bad (= n 0)
             1
             (* n (fact-wrong (- n 1)))))
```

Thunks

We know how to delay evaluation: put expression in a function definition!

- Because defining a function doesn't run the code until later.

A zero-argument function used to delay evaluation is called a *thunk*

- As a verb: *thunk the expression*

This works (though silly to re-define `if` like this):

```
(define (my-if x y z)
  (if x (y) (z)))

(define (fact n)
  (my-if (= n 0)
         (lambda () 1)
         (lambda () (* n (fact (- n 1))))))
```

Try this one

- Write a function called `while` that takes two arguments:
 - a thunk called `condition-thunk`
 - a thunk called `body-thunk`
- This function should emulate a while loop: test the `condition-thunk`, and if it's true, call the `body thunk`. Then test the `condition thunk` again, and if it's still true, run the `body thunk`.
- Write a while loop that prints the numbers 1 to 10.
- Define a function called `my-length` that takes one argument: a list. `my-length` should return the length of the list argument. Use a while loop.

Thunks

- Think of a thunk ☺ as a “promise” to “evaluate this expression as soon as we really need the value.”
- **(define result
 (compute-answer-to-life-univ-and-everything))**
 - Would take a really long time to calculate result.
- **(define result
 (lambda ()
 (compute-answer-to-life-univ-and-everything)))**
 - Note that just by defining a variable to hold the result doesn’t mean we “really” need it yet.
- **(if (= (result) 42)
 (do something) (do something else))**
 - Now we need the value, so we compute it with **(result)**.

Avoiding expensive computations

Thunks let you skip expensive computations if they aren't needed

```
(define result
  (lambda ()
    (compute-answer-to-life-univ-and-everything)))
(if (want-to-know-answer?)
    (display (result)) (display "too bad"))
```

Don't compute the answer to life, the universe, and everything unless you really want to know.

- Pro: More flexible than putting the computation itself inside of the if statement.
- Con: Every time we call **(result)**, we compute the answer again! (Time waste, assuming the answer doesn't change)

```
; simulate a long computation time
(define (compute-answer-to-life)
  (begin (sleep 3) 42))

; create a thunk for the answer
(define answer
  (lambda () (compute-answer-to-life)))

(answer) ; 3 second pause, then 42
(answer) ; 3 second pause again, then 42
```

Best of both worlds

Assuming our expensive computation has no side effects, ideally we would:

- Not compute it until needed
- Remember the answer so future uses don't re-compute
- Known as *lazy evaluation*

Languages where most constructs, including function calls, work this way are *lazy languages*

- Haskell

Racket and Scheme are *eager languages*, but we can add support for laziness.

Delay and force

```
(define (my-delay thunk)
  (mcons #f thunk))
```

```
(define (my-force p)
  (if (mcar p)
      (mcdr p)
      (begin (set-mcar! p #t)
              (set-mcdr! p ((mcdr p)))
              (mcdr p))))
```

my-delay: create a promise data type for the thunk argument.

my-force: return result of thunk (either run it and save the return value for later, or return previously-saved value).

An data structure represented by a mutable pair

- `#f` in car means cdr is an unevaluated thunk
- This data type is called a “promise.” (not language-specific)
 - A promise represents a computation that is either already finished (in which case we remember the answer), or not executed yet (in which case we have some code [as a thunk] for when we need the answer).

Using promises

```
; simulate a long computation time
(define (compute-answer-to-life)
  (begin (sleep 3) 42))

; create a promise to hold a thunk for the answer
(define answer2
  (my-delay
    (lambda () (compute-answer-to-life))))

(my-force answer2) ; 3 second pause, then 42
(my-force answer2) ; instant 42
```

Racket promises

- Making our own promise data structure is still clunky because we have to explicitly wrap everything in a lambda.
- Racket has built-in promises (yay!)
 - (**delay e**): special form that creates a promise to evaluate expression e as soon as its needed.
 - (No extra lambda needed, b/c **delay** is a special form).
 - (**force p**): evaluates a promise (something returned by **delay**) to compute whatever the value of the original expression is. Also caches the value so future forces will be very fast, even if the evaluation of the original expression is slow.

```
(require racket/promise)
(define (compute-answer-to-life)
  (begin (sleep 3) 42))

(define answer3 (delay (compute-answer-to-life)))
(force answer3) ; 3 second pause, then 42
(force answer3) ; instant 42
```

Lazy lists, or streams

- One common use of delayed evaluation is to create a “lazy list,” or a “stream.”
- A stream is just like a list (a Racket list) in that it consists of two parts: the car and the cdr.
 - Only difference is that the cdr is lazy (car is not usually lazy)
 - In other words, the cdr is a promise to return the rest of the stream when its really needed.
- We need a new function to make a pair where the car is normal but the cdr is lazy.

Streams

- **stream-cons**: a special form that creates a new pair where the car is eager but the cdr is lazy
 - alternatively, think of this as creating a new stream from a new first element and an existing stream
 - just like regular cons creates a new list from a new first element and an existing list:
 - (cons 1 '(2 3 4 5)) → '(1 2 3 4 5)
- **(define (stream-cons first rest)**
 (cons first (delay rest))
the above definition is correct in spirit, though wrong in syntax because we need to make stream-cons a special form so that rest will be thunked automatically.

Streams

```
(define the-empty-stream '())
```

```
(define (stream-null? stream)  
  (null? stream))
```

```
(define (stream-car stream)  
  (car stream))
```

```
(define (stream-cdr stream)  
  (force (cdr stream)))
```

Let's try it out