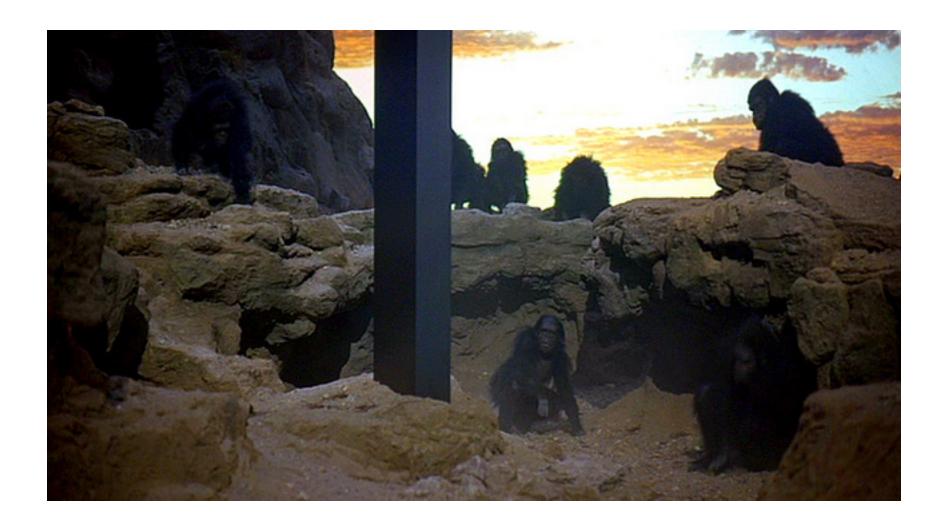
# **Programming Languages**

First Class Functions

Material adapted from Dan Grossman's PL class, U. Washington



#### Today's lecture will take your programming skills from this...



#### ...to this!



## An Example

What if we wanted to add up all the numbers from a to b?

```
(define (sum a b)
(if (> a b))
0
(+ a)
(sum (+ a 1) b))))
i=a
```

## An Example

 What if we wanted to add up the sum of the squares of the numbers from a to b:

```
(define (sum-squares a b)

(if (> a b)
0
(+ (expt a 2)
(sum-squares (+ a 1) b))))

i=a
```

## An Example

 What if we wanted to add up the sum of the square roots of the numbers from a to b:

```
(define (sum-square-roots a b)

(if (= a b)
0
(+ (sqrt a)
(sum-square-roots (+ a 1) b))))

i=a
```

# These functions are all very similar

- All three of these functions differ only in how the sequence of integers from a to b are transformed before they are all added together.
- The adding process itself is identical in all of the functions:

 What if there were a general sum function that could sum up any sequence of this form?

#### A function that takes a function

 Here's a general purpose sum function that takes an argument, called func, that will be applied to each element in the sequence from a to b before the elements are summed:

#### Sum-any in action!

```
(sum-any sqrt 1 10)
 => sqrt(1) + sqrt(2) + sqrt(3) + ...
 => about 22.5
(define (square x) (* x x))
(sum-any square 1 4)
 => 1^2 + 2^2 + 3^2 + 4^2 => 1 + 4 + 9 + 16 => 30
(define (identity x) x)
(sum-any identity 1 4)
 => 10
```

#### How to use sum-any

 You can put the name of any function in place of sqrt, square, or identity, and sum-any will compute

$$f(a) + f(a + 1) + f(a + 2) + ... + f(b)$$

- Provided f is a function of a single numeric argument.
- What if you want to compute  $f(a^2/2) + f((a+1)^2/2) + ...$ 
  - Fine to do:

```
(define (silly-function x) (/ (* x x) 2)) (sum-any silly-function 1 10)
```

But this is better:

```
(sum-any (lambda (x) (/ (* x x) 2)) 1 10)
```

- Recall that lambda creates an anonymous function:
  - (lambda (arg1 arg2...) expression)

```
(define (sum-any func a b) . . . )
(sum-any square 1 10)
(sum-any sqrt 3 5)
(sum-any identity -8 80)
(sum-any (lambda (x) (/ (* x x) 2)) 1 10)
```

## Using anonymous functions

- Most common use: Argument to a higher-order function
  - Don't need a name just to pass a function
- But: Cannot use an anonymous function for a recursive function
  - Because there is no name for making recursive calls

```
(define (triple x) (* 3 x); named version
(lambda (x) (* 3 x)) ; anonymous version
```

# Named functions vs anonymous functions

- Named functions are mostly indistinguishable from anonymous functions.
- In fact, naming a function with define uses the anonymous form behind the scenes:

```
(define (func arg1 arg2 ...) expression)
is converted to:
  (define func (lambda (arg1 arg2 ...) expression))
```

- It is poor style to define unnecessary functions in the global (toplevel) environment
  - Use either nested defines, or anonymous functions.

## Higher-order functions

- A higher-order function is a function that either takes a function (or more than one function) as an argument, or returns a function as a return value.
- Possible because functions are first-class values (or first-class citizens), meaning we can use a function wherever we use a value.
  - Arguments, results of functions, elements of lists, bound to variables, etc
- Most common use is as an argument / result of another function

## Higher-order functions

Let's see another:

```
(define (do-n-times func n x)
  (if (= n 0) x
      (do-n-times func (- n 1) (func x))))
```

• This function computes f(f(f...(x))), where the number of applications of f is n.

#### Some uses for do-n-times

Get-nth:

```
- (define (get-nth lst n)
          (car (do-n-times cdr n lst)))
```

Exponentiation:

```
- (define (power x y); raise x to the y power (do-n-times (lambda (a) (* x a)) y 1))
```

- Note how in the exponentiation example, the anonymous function uses variable x from the outer environment.
  - Couldn't do that without being able to nest functions.
- Note how do-n-times can work with any data type (e.g., lists, numbers...)

# A style point

Compare:

(if x #t #f)

With:

(lambda (x) (f x)

So don't do this:

```
(do-n-times (lambda (x) (cdr x)) 3 '(2 4 6 8))
```

When you can do this:

```
(do-n-times cdr 3 '(2 4 6 8))
```

#### What does this function do?

```
(define (mystery lst)
  (if (null? lst) '()
      (cons (car lst) (mystery (cdr lst)))))
```

# Map

```
(define (map func lst)
  (if (null? lst) '()
     (cons (func (car lst)) (map func (cdr lst)))))
```

Map is, without doubt, in the higher-order function hall-of-fame

- The name is standard (same in most prog languages)
- You use it all the time once you know it: saves a little space,
   but more importantly, communicates what you are doing
- Built into Racket, so you don't have to include this definition in programs that use map.

#### Filter

Filter is also in the hall-of-fame

So use it whenever your computation is a filter